GCE Examinations

Advanced Subsidiary / Advanced Level

Mechanics
Module M3

Paper A

MARKING GUIDE

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks should be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.

Accuracy marks (A) can only be awarded when a correct method has been used.

(B) marks are independent of method marks.



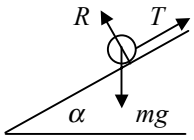
Written by Shaun Armstrong & Chris Huffer

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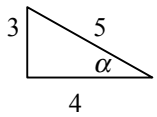
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M3 Paper A – Marking Guide

1. *(a)* $T = \frac{\lambda x}{l} = \frac{30\times0.2}{1} = 6$ N — M1 A1

(b) 

resolve ↗: $T - mg\sin\alpha = ma$ — M1 A1



$\therefore \sin\alpha = \frac{3}{5}$ — M1

$\therefore\ 6 - 0.6\times9.8\times\frac{3}{5} = 0.6a$ — M1

giving $a = 4.12$ ms^{-2} — A1 **(7)**

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2. *(a)* $F = ma = 0.5\,v\frac{dv}{dx} = 3x^{\frac{1}{2}}$ — M1

$\therefore \int v\ dv = \int 6x^{\frac{1}{2}}\ dx$ — M1

giving $\frac{1}{2}v^2 = 4x^{\frac{3}{2}} + c$ — A1

$x = 1, v = 2\ \therefore c = -2$ — M1

$\therefore v^2 = 8x^{\frac{3}{2}} - 4$ — A1

(b) $x = 4$ gives $v^2 = 64 - 4 = 60\ \therefore v = \sqrt{60} = 7.7$ ms^{-1} (1dp) — M1 A1 **(7)**

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3. *(a)* amplitude $= \frac{1}{2}\times8 = 4$ m — B1

period $= \frac{2\pi}{\omega} = 12\ \therefore \omega = \frac{\pi}{6}$ — B1

$v_{max} = a\omega = 4\times\frac{\pi}{6} = \frac{2\pi}{3}$ ms^{-1} — M1 A1

(b) $x = a\sin\omega t$ — M1

at P, $-1 = 4\sin\omega t\ \therefore \frac{\pi}{6}t = -0.2527,\ t = -0.4826$ — M1 A1

at Q, $2 = 4\sin\omega t\ \therefore \frac{\pi}{6}t = \frac{\pi}{6},\ t = 1$ — M1 A1

$\therefore$ time between = 1.48 s (3sf) — A1 **(10)**

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4. *(a)* $v^2 = kg - kg\,e^{-\frac{2x}{k}}\ \therefore 2v\frac{dv}{dx} = 2g\,e^{-\frac{2x}{k}}$ — M1 A2

$f =$ accel. $= v\frac{dv}{dx} = g\,e^{-\frac{2x}{k}}$ — A1

(b) when x is large, $e^{-\frac{2x}{k}} \to 0$ — M1

$\therefore 49^2 = kg$ giving $k = \frac{49^2}{9.8} = 245$ — M1 A1

(c) $v^2 = kg - kg\,e^{-\frac{2x}{k}} = kg - kf$ — M1 A1

$\therefore f = g - \frac{1}{k}v^2 = 9.8 - \frac{1}{245}v^2$ — M1 A1 **(11)**

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5. *(a)*

portion	mass	y	my
cone	$\rho\times\frac{1}{3}\pi r^2(2r) = \frac{2}{3}\rho\pi r^3$	$h+\frac{1}{4}(2r)=h+\frac{1}{2}r$	$\frac{2}{3}\rho\pi r^3(h+\frac{1}{2}r)$
cylinder	$\rho\pi r^2 h$	$\frac{1}{2}h$	$\frac{1}{2}\rho\pi r^2 h^2$
firework	$\rho\pi r^2(h+\frac{2}{3}r)$	$\bar{y}$	$\rho\pi r^2(\frac{1}{2}h^2+\frac{2}{3}rh+\frac{1}{3}r^2)$

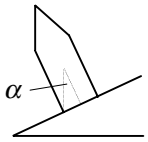
ρ = mass per unit volume y coords. taken vert. from base — M2 A4

$\rho\pi r^2(h+\frac{2}{3}r)\times\bar{y} = \rho\pi r^2(\frac{1}{2}h^2+\frac{2}{3}rh+\frac{1}{3}r^2)$ — M1

$\therefore\ 2(3h+2r)\times\bar{y} = 3h^2+4rh+2r^2$ — M1

giving $\bar{y} = \frac{3h^2+4hr+2r^2}{2(3h+2r)}$ — A1

(b)



$h = 4r\ \therefore\ \bar{y} = \frac{33}{14}r$ — M1

$\tan\alpha = r\div(\frac{33}{14}r) = \frac{14}{33}$ — M1 A1

$\therefore\ \alpha = 23°$ (nearest degree) — A1 **(13)**

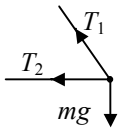
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6. *(a)* string taut $\therefore\ PR = a,\ PR^2+QR^2 = a^2+3a^2 = 4a^2 = PQ^2$ — M1

by converse of Pythag. $\angle PRQ = 90°$ — A1

(b) $\sin\angle PQR = \frac{a}{2a} = \frac{1}{2}\ \therefore\ \angle PQR = 30°$ — B1

(c) (i)



resolve ↑: $T_1\sin 60 - mg = 0$ — M1 A1

$\therefore\ T_1 = \frac{2mg}{\sqrt{3}}$ (or $\frac{2}{3}\sqrt{3}\,mg$) — A1

(ii) resolve ←: $T_2 + T_1\cos 60 = \frac{mv^2}{r}$ — M1 A1

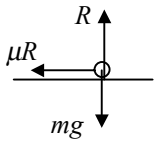
$\therefore\ T_2 = \frac{mu^2}{a} - \frac{1}{2}\times\frac{2mg}{\sqrt{3}} = \frac{mu^2}{a} - \frac{mg}{\sqrt{3}}$ (or $\frac{mu^2}{a} - \frac{1}{3}\sqrt{3}\,mg$) — M1 A1

(d) PR taut $\therefore\ T_2 \geq 0$ — M1

giving $\frac{mu^2}{a} \geq \frac{mg}{\sqrt{3}}$ so $u^2 \geq \frac{ga}{\sqrt{3}}$ — M1 A1 **(13)**

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7. *(a)*



resolve ↑: $R - mg = 0\ \therefore\ R = 2g$ — M1 A1

friction $= \mu R = \frac{10}{49}\times 2\times 9.8 = 4$ — A1

work-energy:

work done = loss of KE − gain of EPE — M1

$\therefore\ Fs = \frac{1}{2}mu^2 - \frac{\lambda x^2}{2l}$ — M1

so $4d = \frac{1}{2}\times 2\times 5^2 - \frac{50(d-1)^2}{2\times 1}$ — A1

$\therefore\ 4d = 25 - 25(d^2-2d+1)$ — M1

giving $25d^2 - 46d = 0,\ d(25d-46) = 0$ — M1

$\therefore\ d = 0$ (initially) or $\frac{46}{25} = 1.84$ m — A1

(b) work-energy: work done = loss of EPE − gain of KE — M1

$\therefore\ 4\times\frac{46}{25} = \frac{50\times(\frac{21}{25})^2}{2\times 1} - \frac{1}{2}\times 2\times v^2$ — M1 A1

giving $21^2 = (4\times 46) + 25v^2$ — M1

so $v^2 = \frac{257}{25}\ \therefore\ v = 3.2\ \text{m s}^{-1}$ (2sf) — A1 **(14)**

Total **(75)**

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Performance Record – M3 Paper A

Question no.	**1**	**2**	**3**	**4**	**5**	**6**	**7**	Total
Topic(s)	elastic spring	variable force	SHM	variable accel.	centre of mass, equilm.	circular motion	elastic string, EPE, work done	
Marks	7	7	10	11	13	13	14	75
Student								

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